

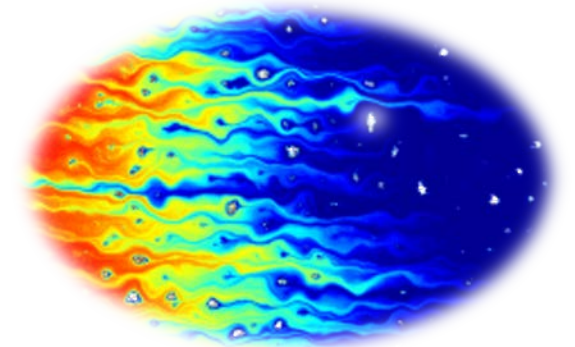
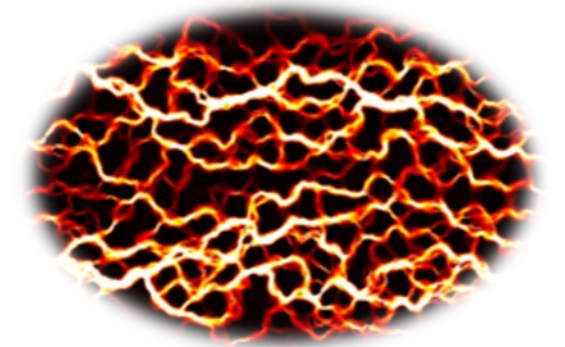
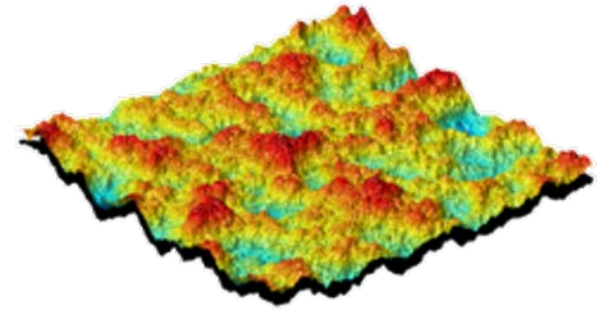
Experimental Investigations of Flow and Mass Transport in Stressed Rough Fractures

Rafael Villamor-Lora

PhD Student, Civil & Environmental Engineering

In collaboration with Herbert H. Einstein

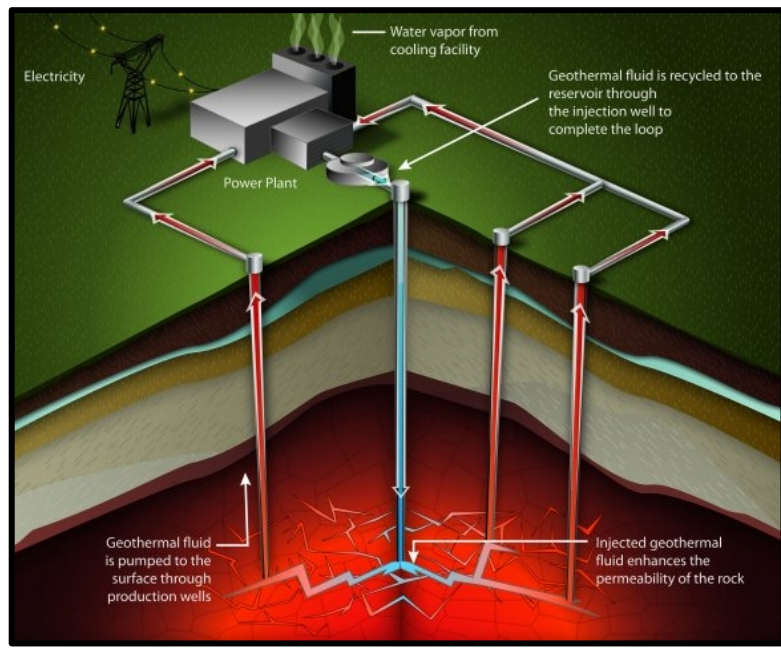
May 25, 2022



Motivation

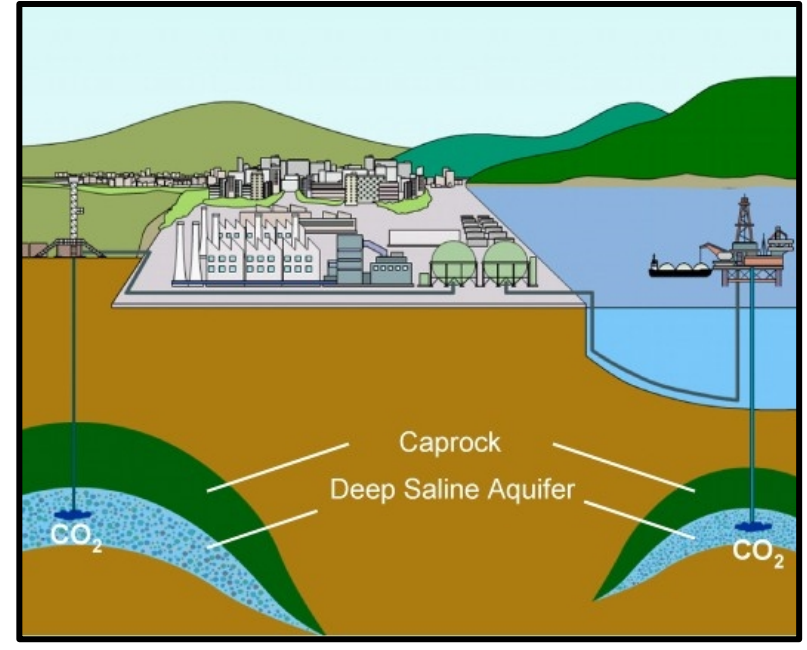
Flow in Rough Fractures. Applications

Geothermal Energy



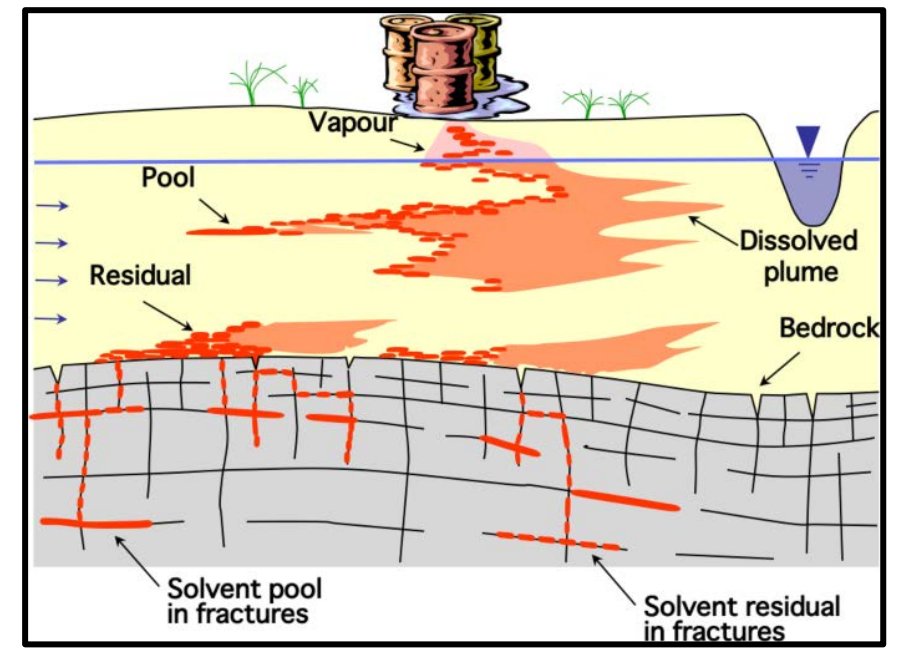
Source: [Department of Energy](#)

CO2 Sequestration



Source: [Yohanes Nuwara](#)

Contaminant Transport

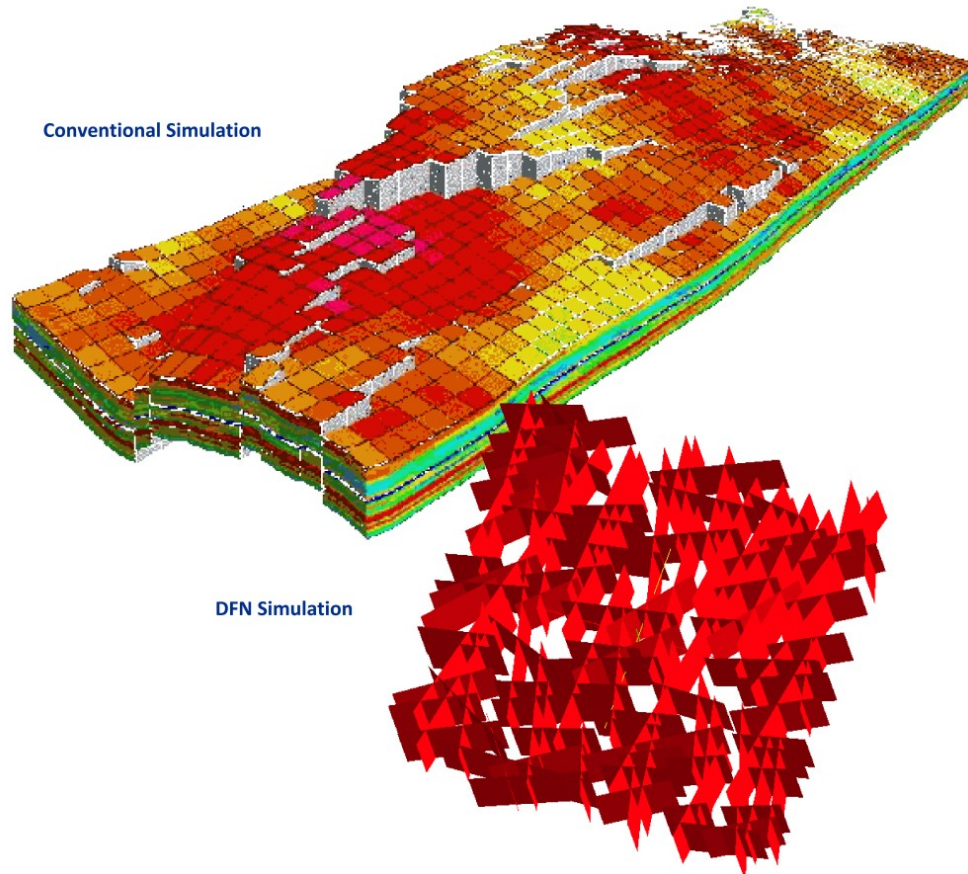


Source: [Lehane \(2019\), ChemTexts](#)

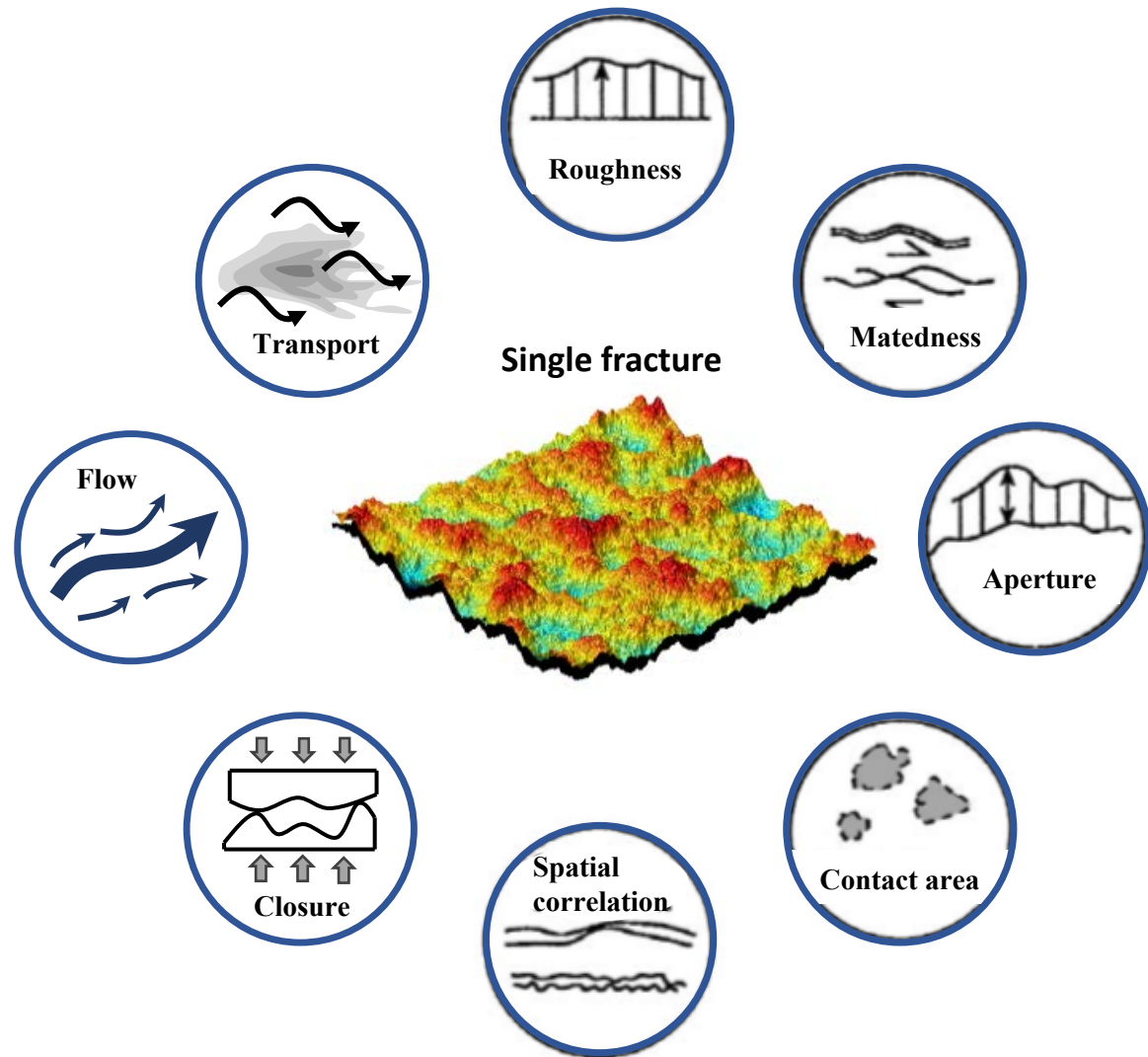
Others: Oil & Gas, Biotechnology, etc.

Motivation

COUPLED PHYSICAL PROCESSES IN STRESSED, ROUGH FRACTURES



Source: [iReservoir](#)

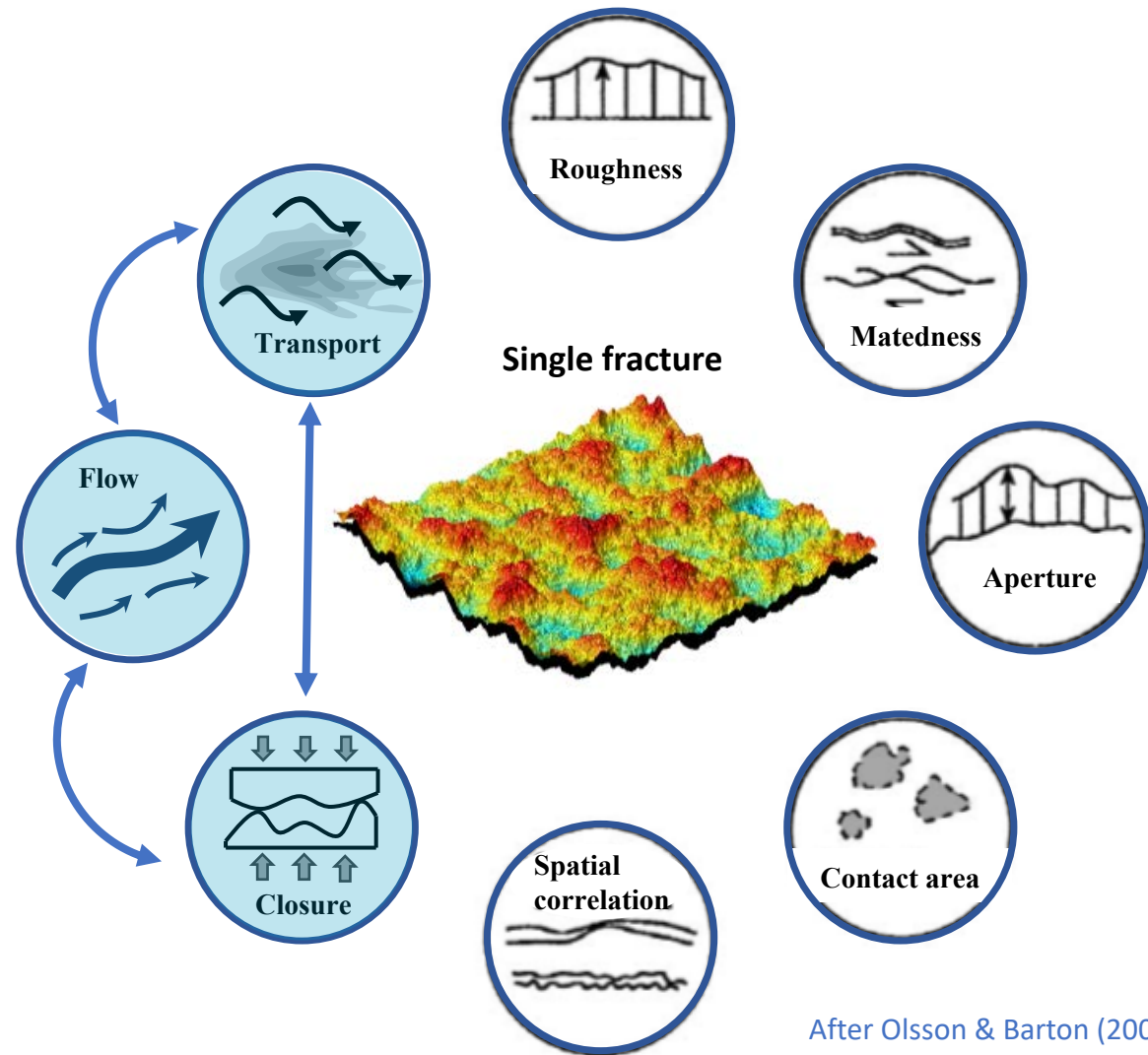


Motivation

COUPLED PHYSICAL PROCESSES IN STRESSED, ROUGH FRACTURES



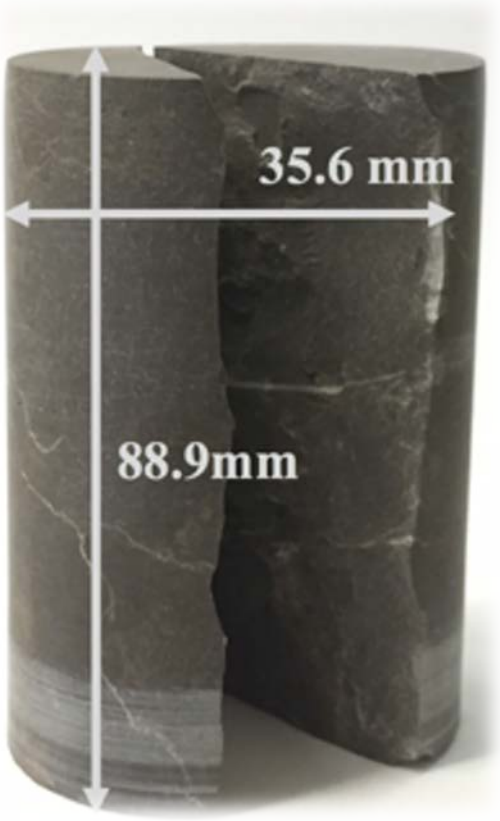
- Experimentally investigate the interplay between **fracture deformation & flow & mass transport**
- Develop an experimental setup that allows direct **visualization** of different physical processes **under stress at real time**



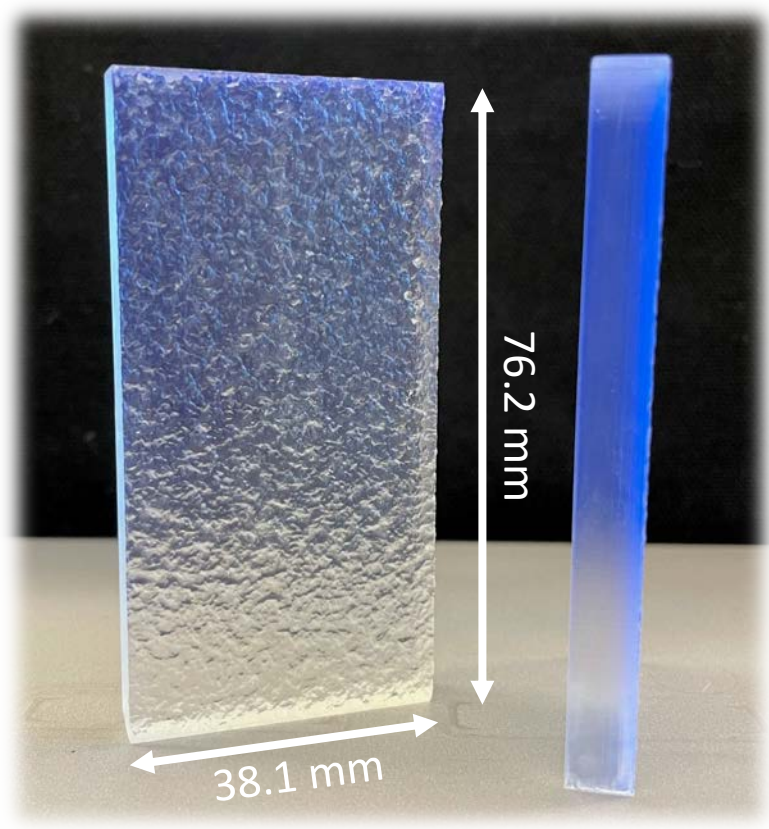
After Olsson & Barton (2001)



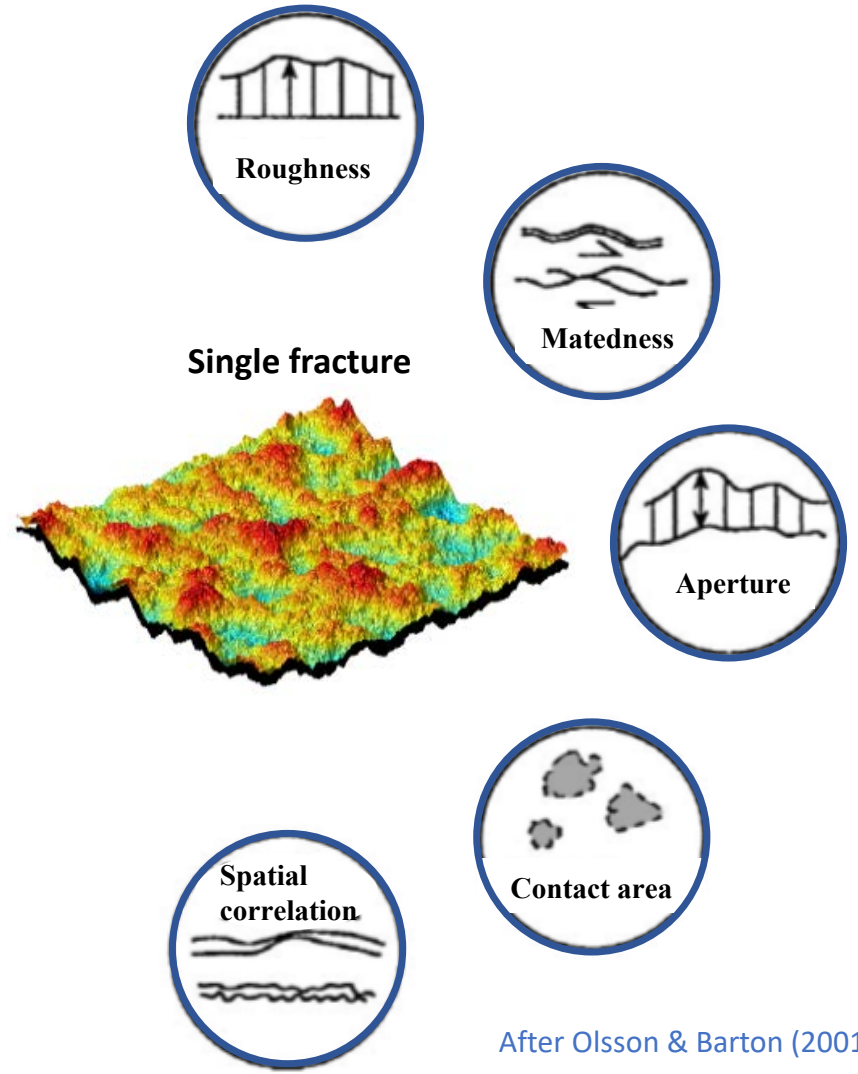
Experimental Investigations



Real rock fractures
[Musandam limestone]



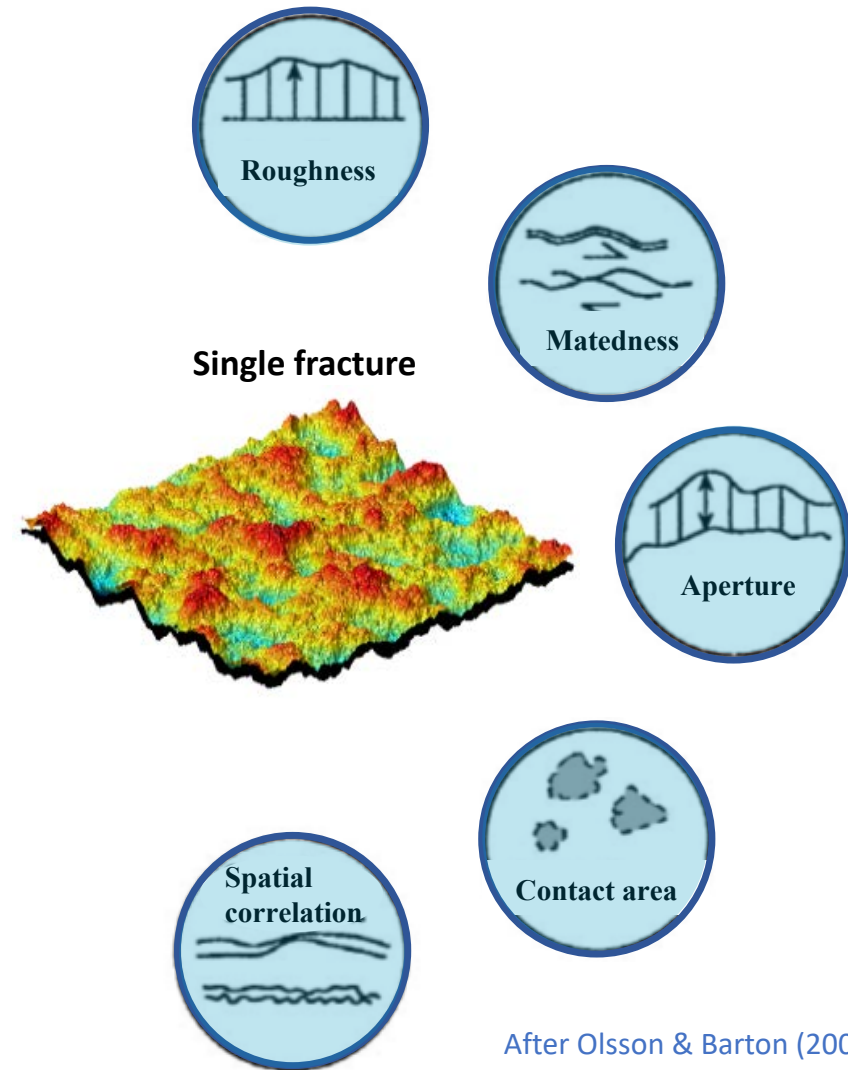
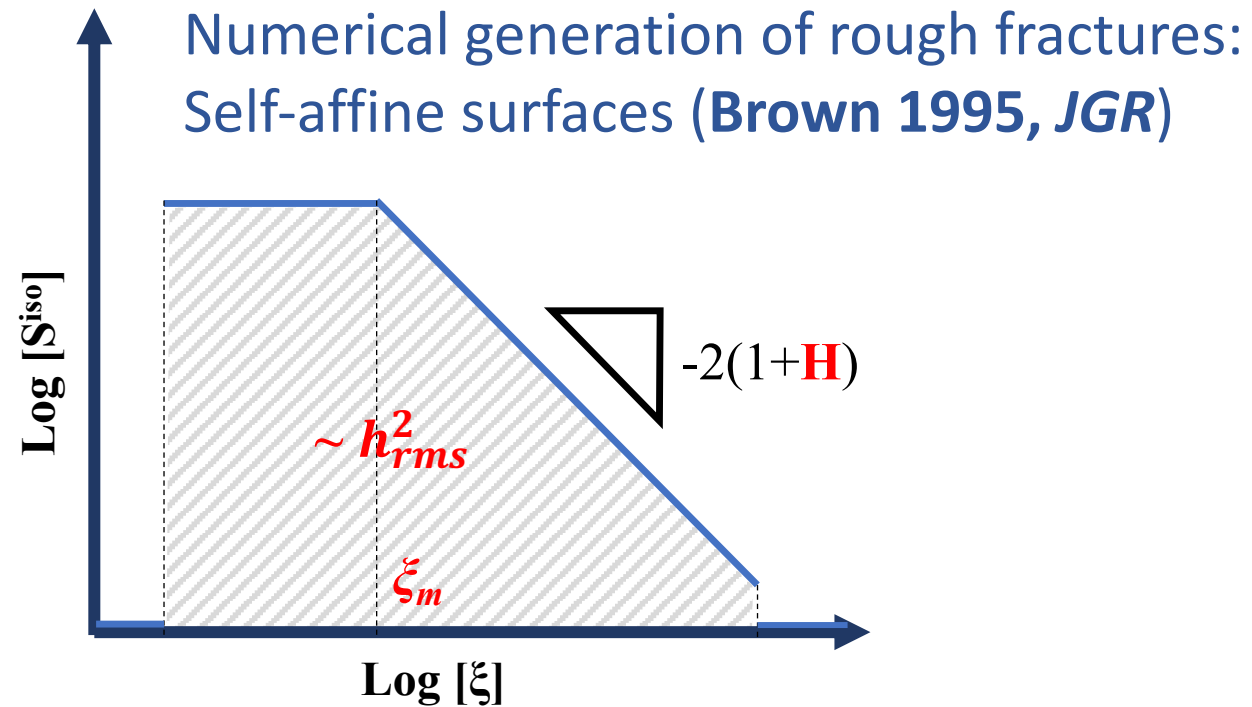
3D-printed fracture analogs



After Olsson & Barton (2001)

Experimental Investigations

DIGITAL FABRICATION OF ROUGH ROCK FRACTURES

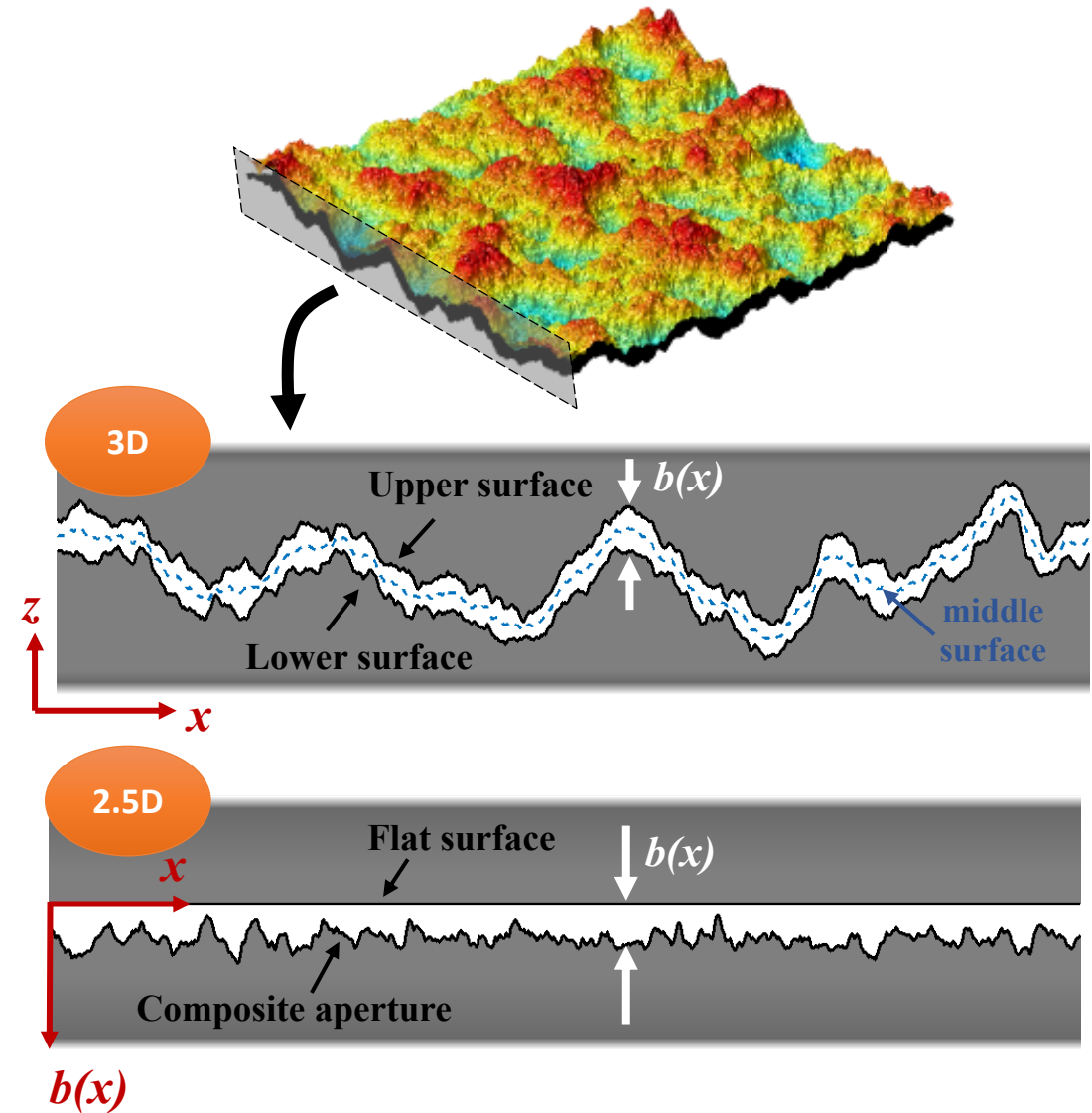
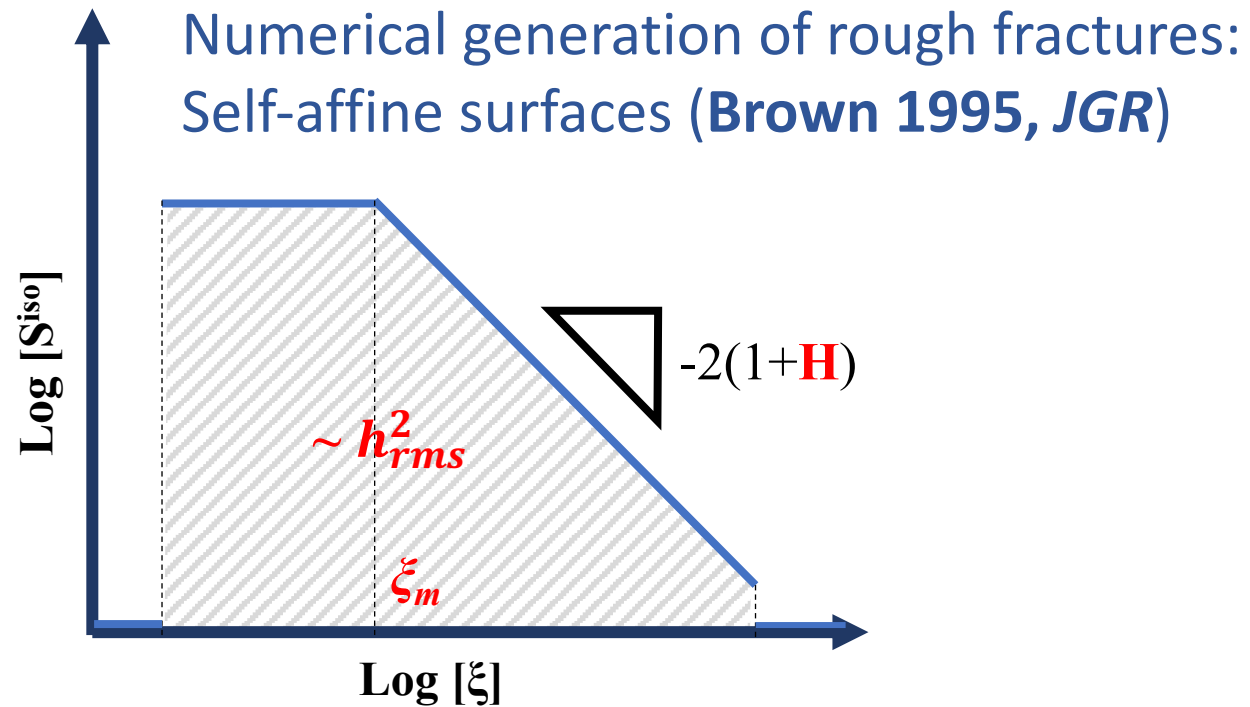


After Olsson & Barton (2001)



Experimental Investigations

DIGITAL FABRICATION OF ROUGH ROCK FRACTURES

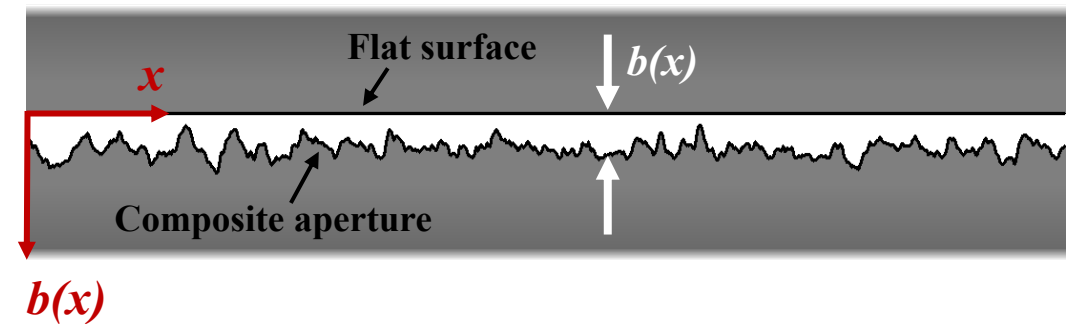
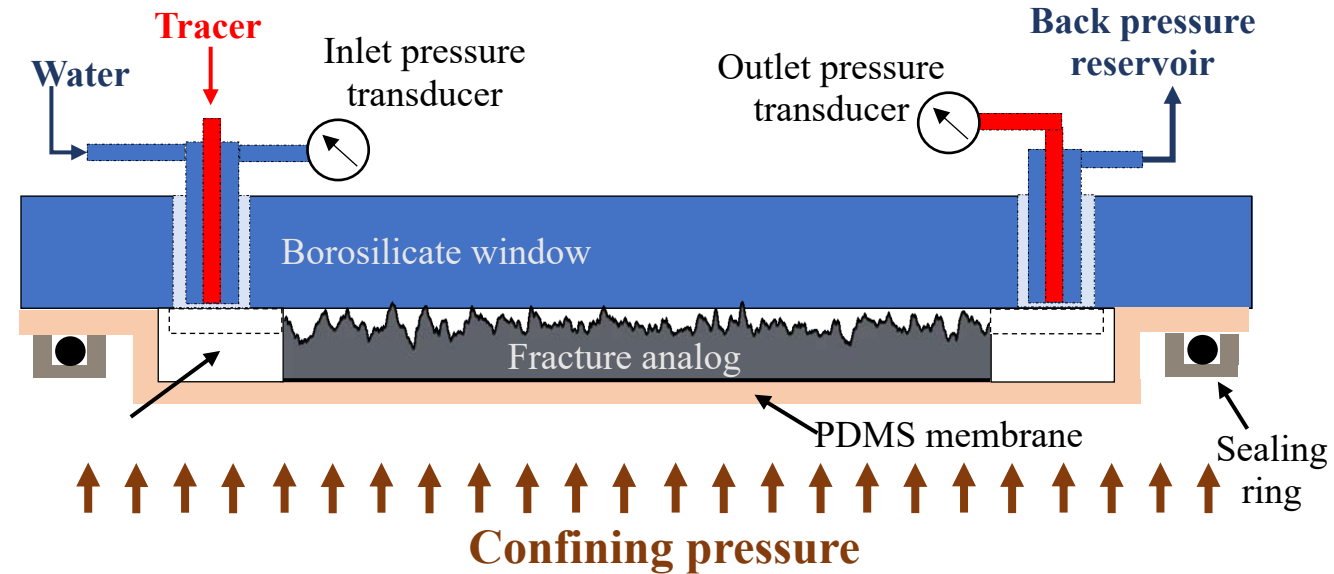
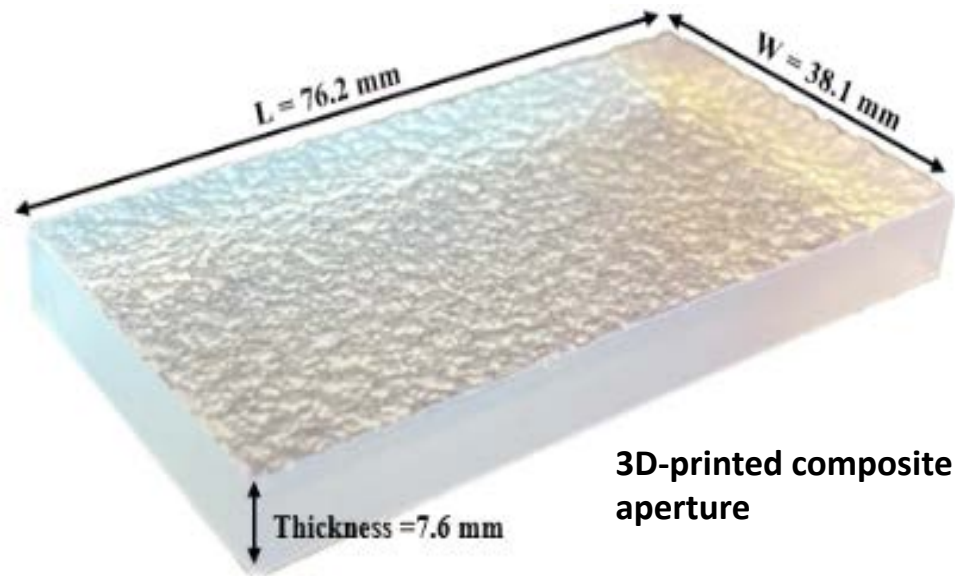


Experimental Investigations

PRESSURE-CONTROLLED HELE-SHAW CELL

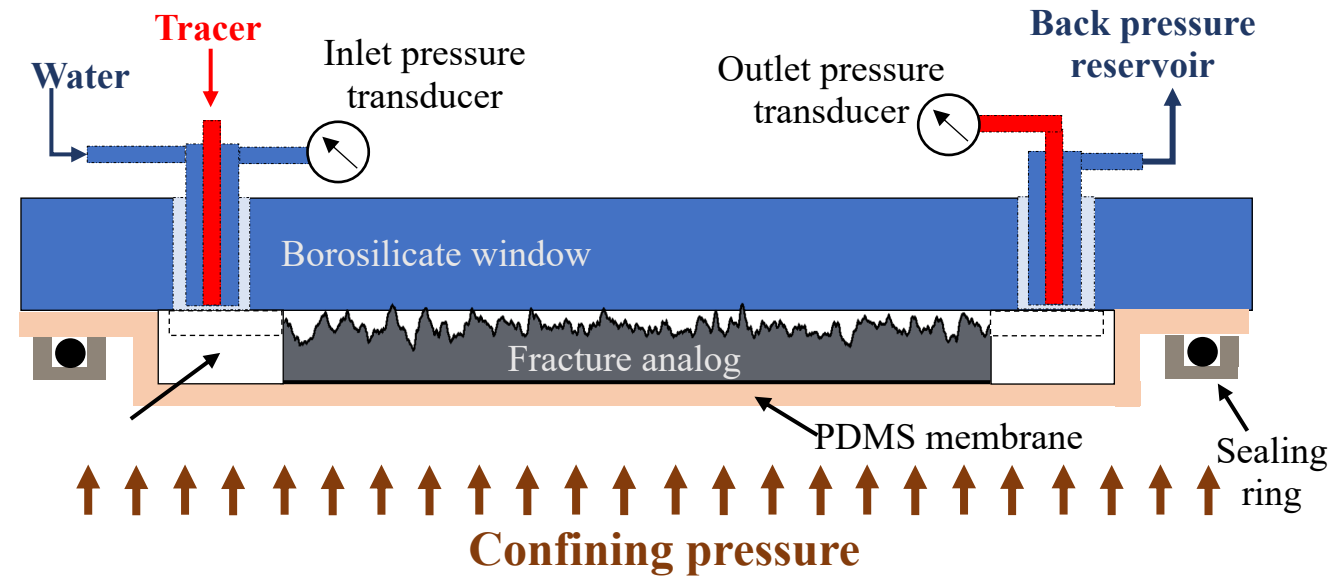
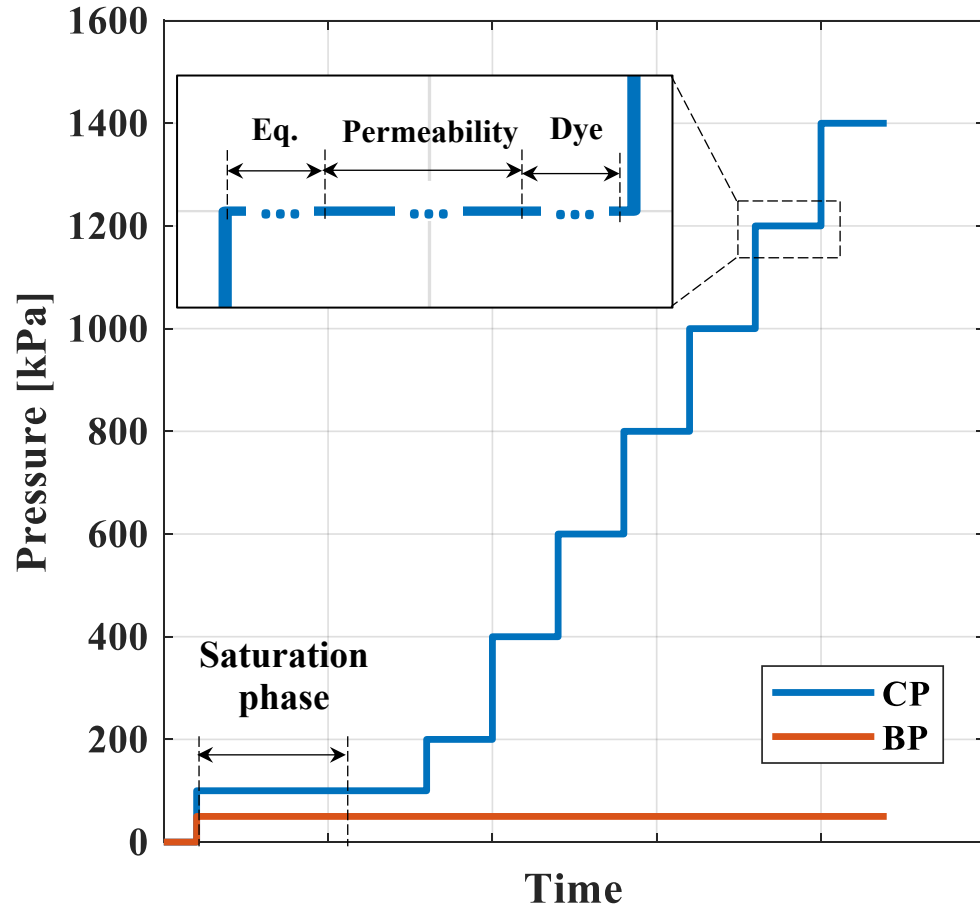
Lab-Field scaling

$$\sigma_{lab} / E_{lab} \sim \sigma_{field} / E_{field}$$



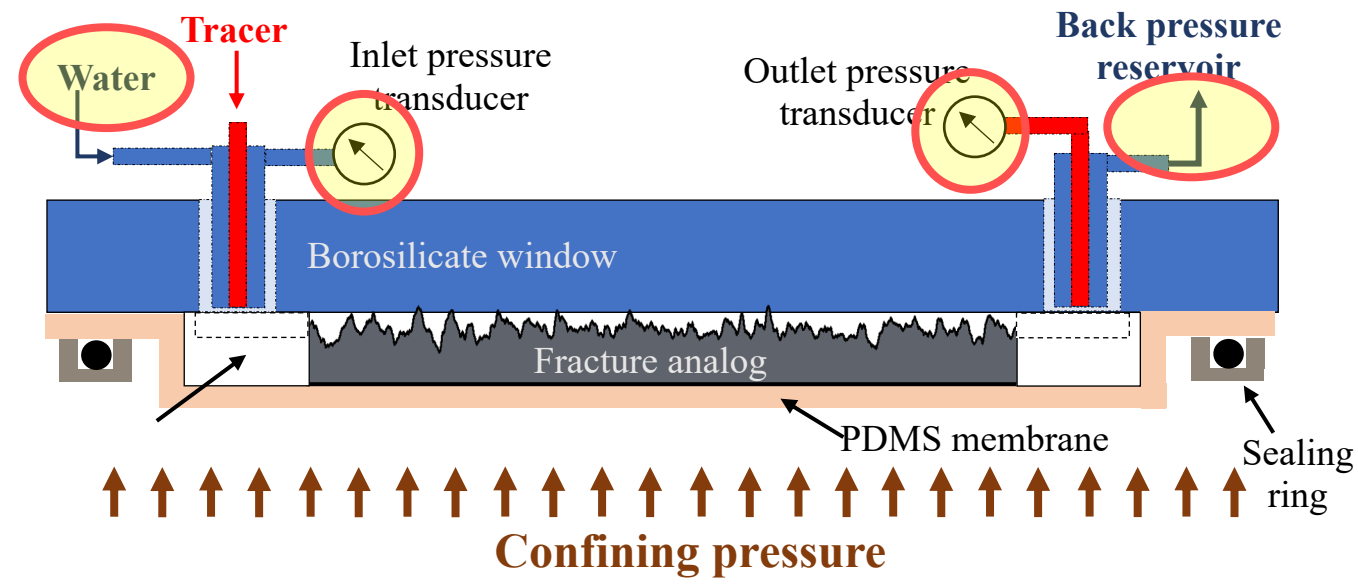
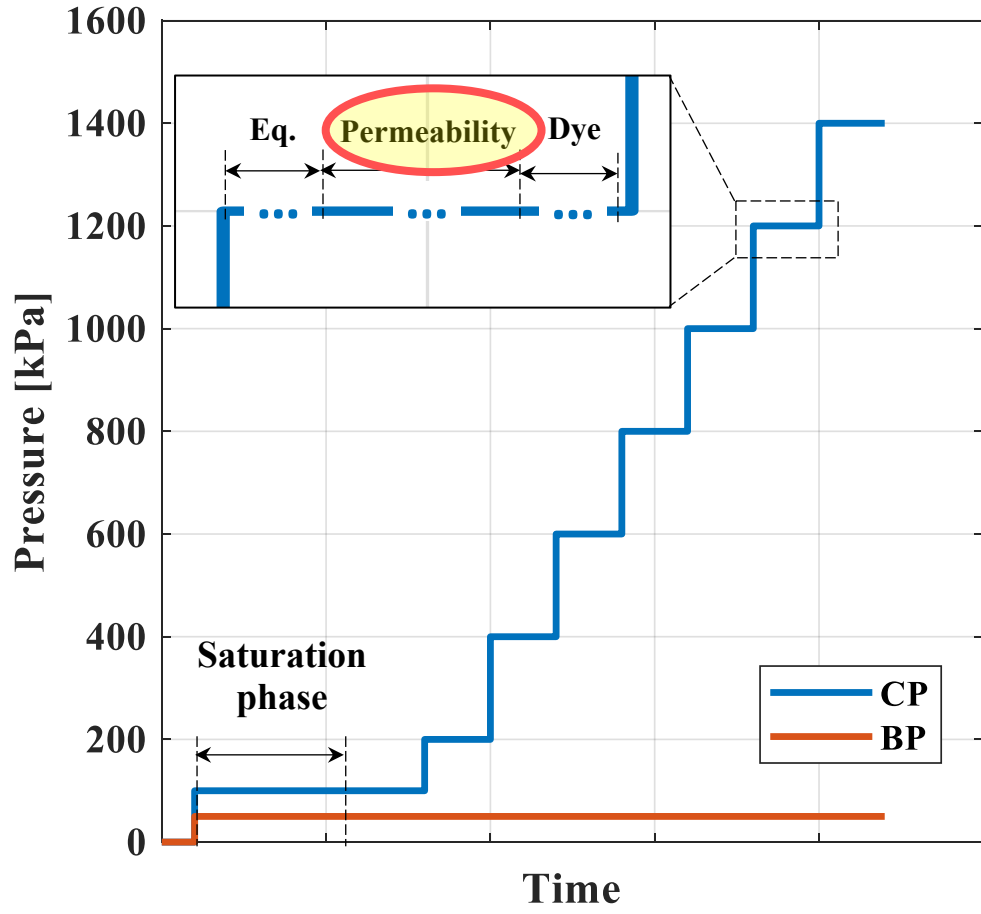
Experimental Investigations

EXPERIMENTAL PROTOCOL



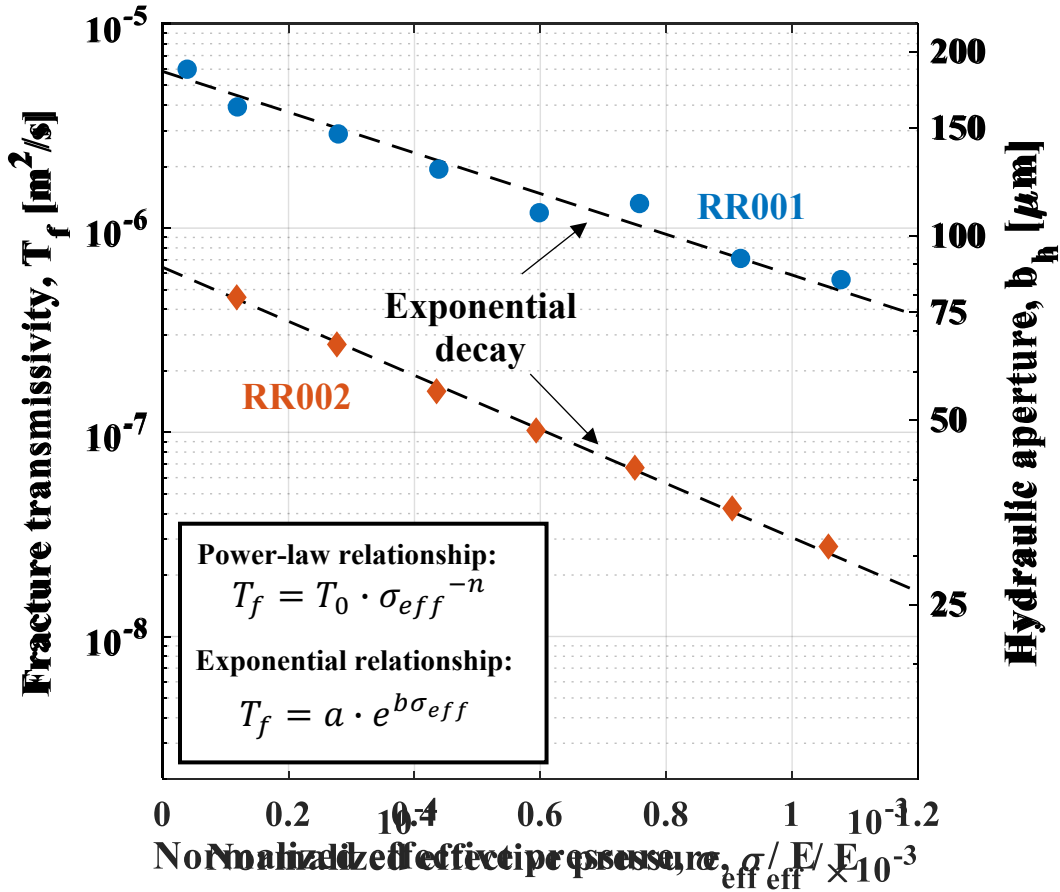
Experimental Investigations

HYDRAULIC MEASUREMENTS (PERMEABILITY)



Experimental Investigations

HYDRAULIC MEASUREMENTS (PERMEABILITY)



Fracture transmissivity

$$T_j = \rho g \frac{Q}{\Delta P} \frac{L}{W}$$

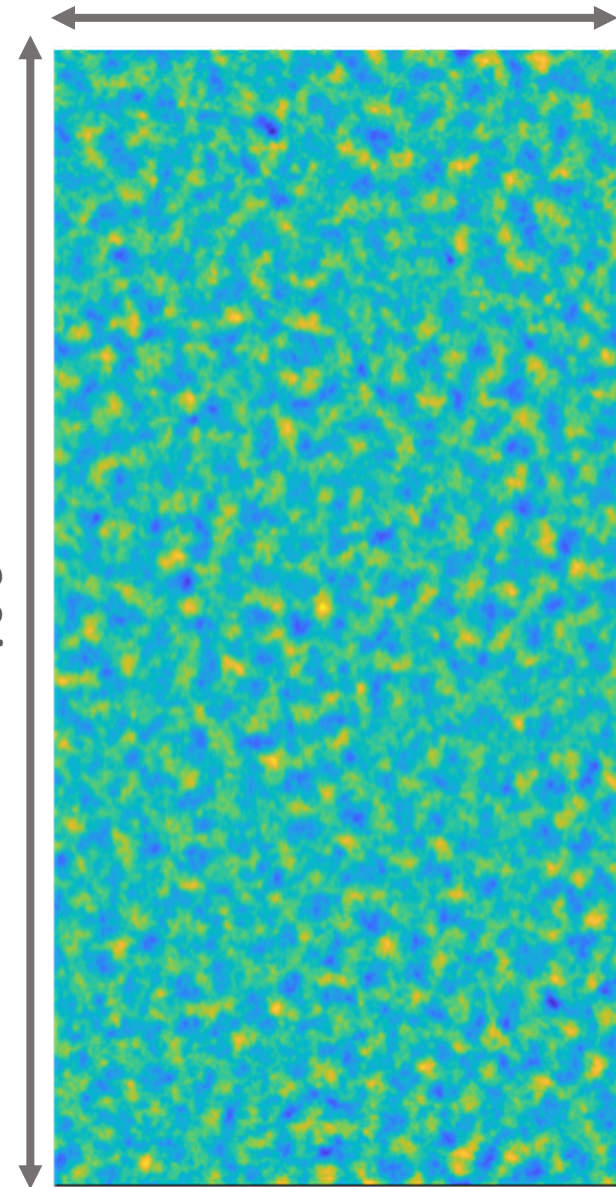
Hydraulic aperture

$$b_h = \sqrt[3]{12\mu \frac{Q}{\Delta P} \frac{L}{W}}$$

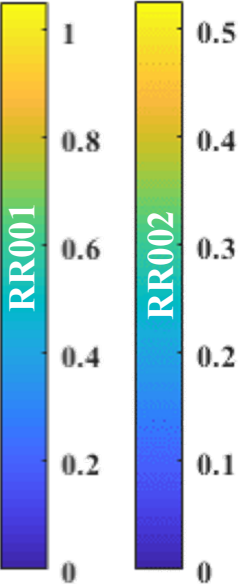
- ρ Fluid density
- g Gravity acceleration
- Q Flow rate
- ΔP Pressure drop
- L Fracture length
- W Fracture width

3.0 in

1.5 in

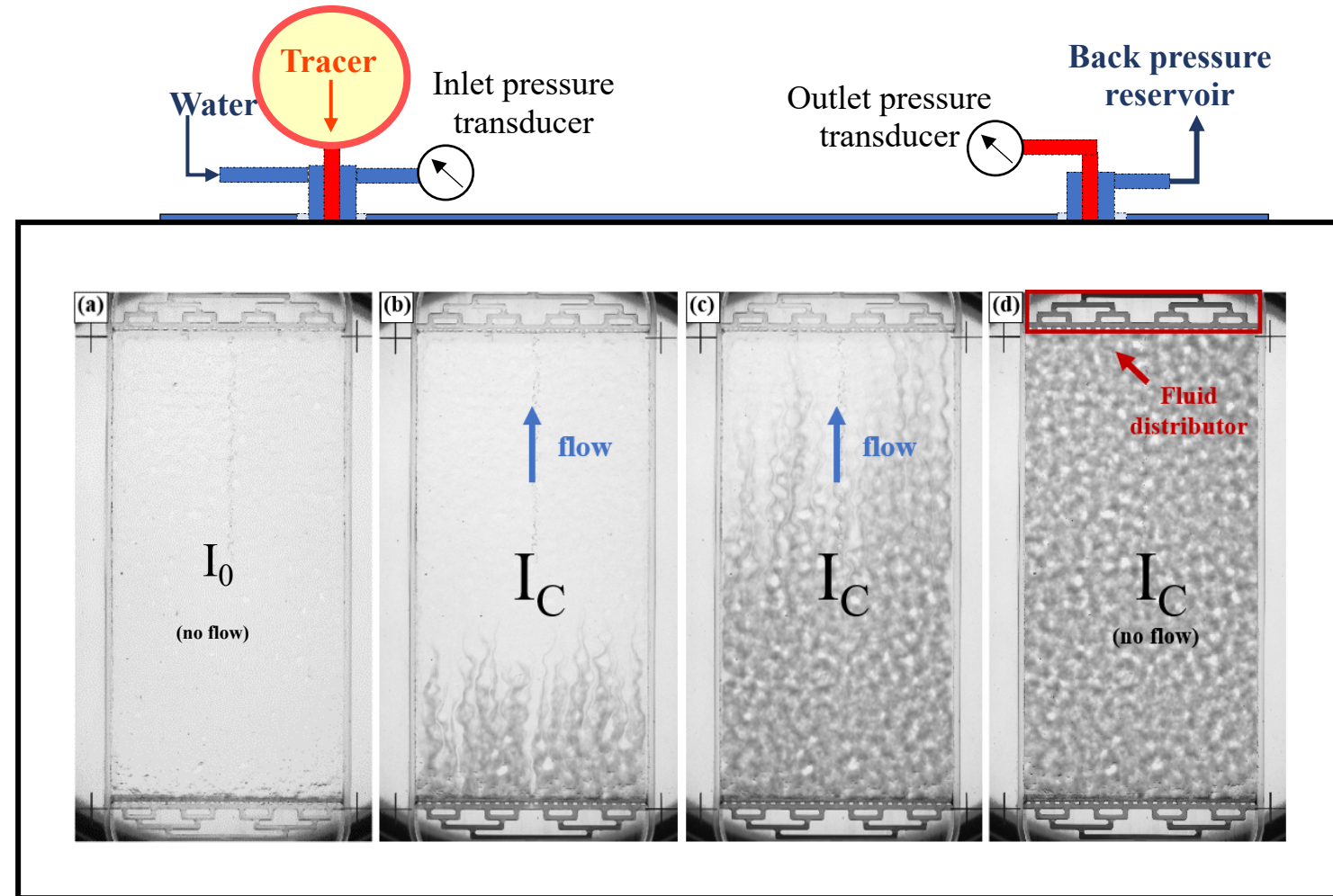
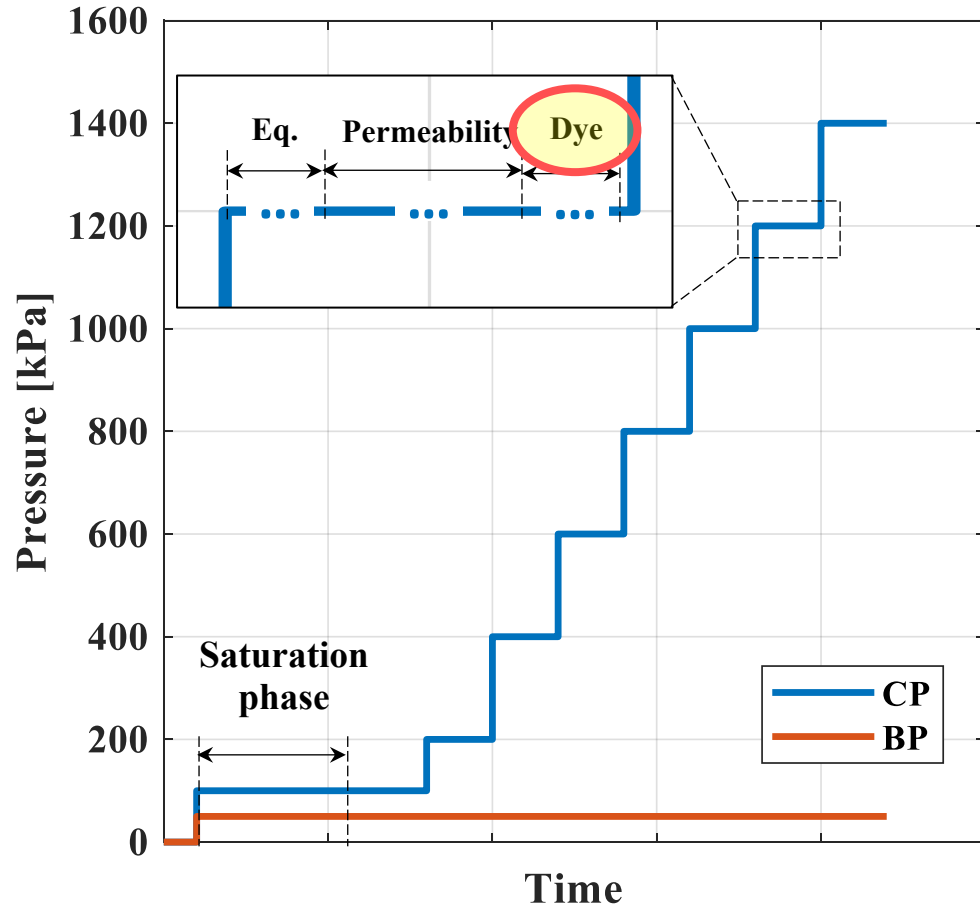


Depth [mm]



Experimental Investigations

FRACTURE DEFORMATION & MASS TRANSPORT



Light intensity

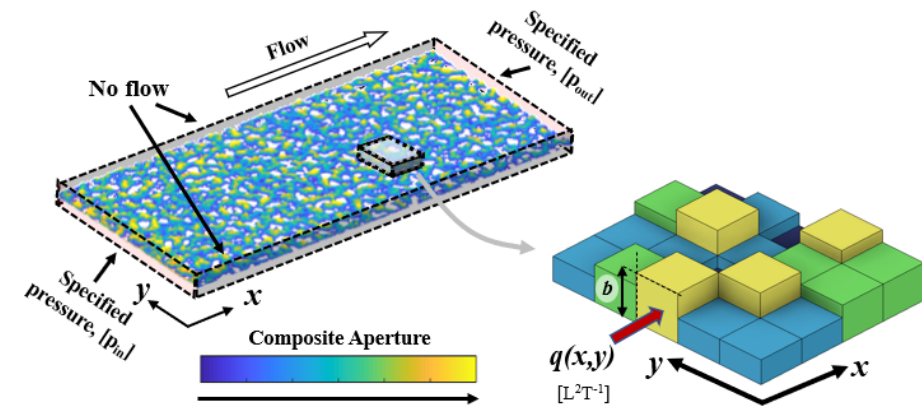
Beer-Lambert Law



Aperture & Concentration maps

Flow simulations

DETERMINATION OF THE FLOW FIELD: LOCAL CUBIC LAW



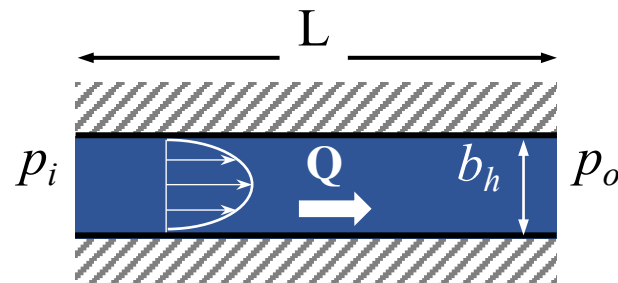
Local Cubic Law: LCL

$$\nabla \cdot \vec{q} = 0$$

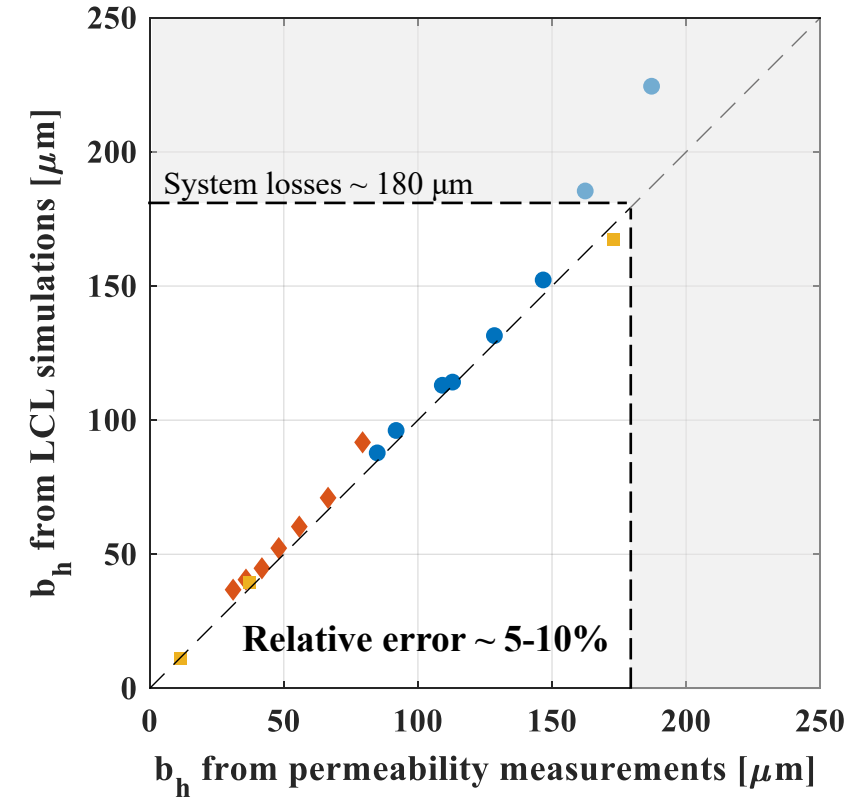
q : local flux

b : local aperture

$$\vec{q} = \frac{b^3}{12\mu} \nabla p$$



Simulations vs. Experiments



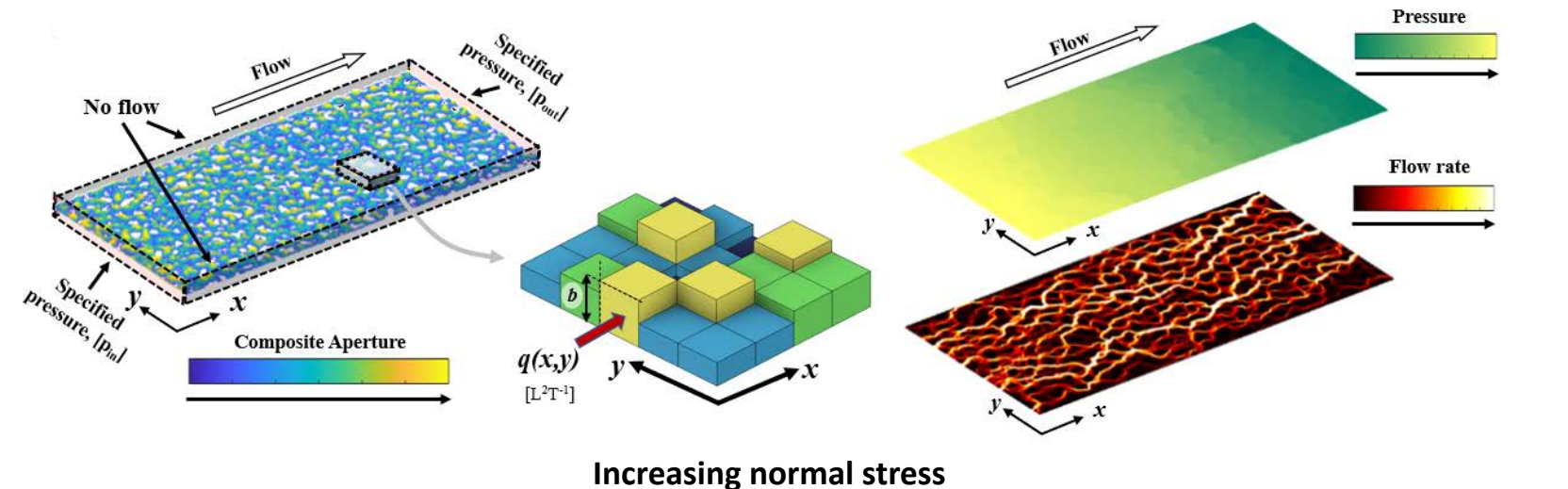
Hydraulic aperture

$$b_h = \sqrt[3]{12\mu \frac{Q}{\Delta P} \frac{L}{W}}$$

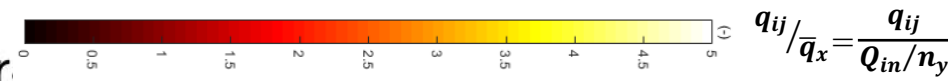
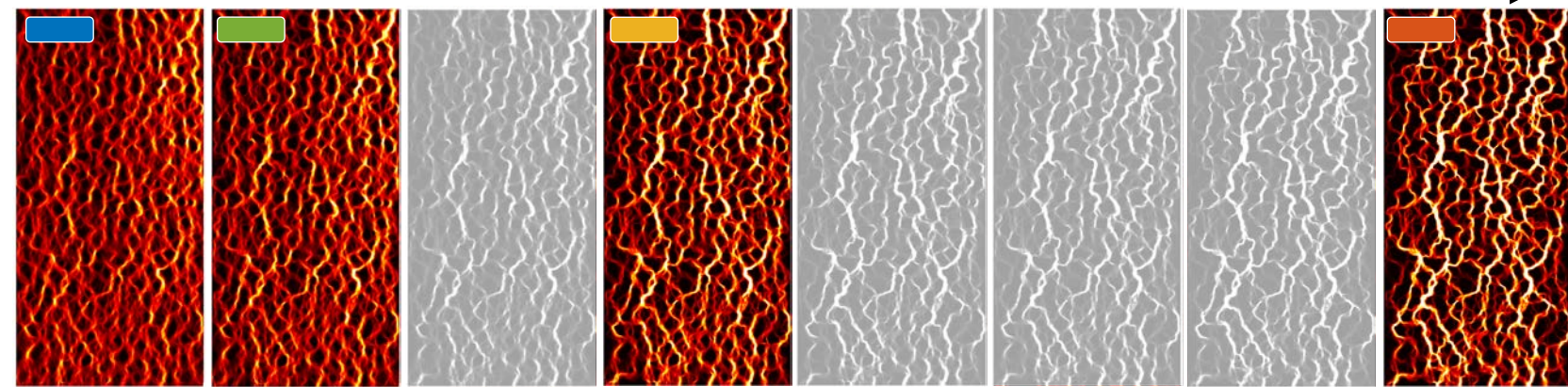


Flow simulations

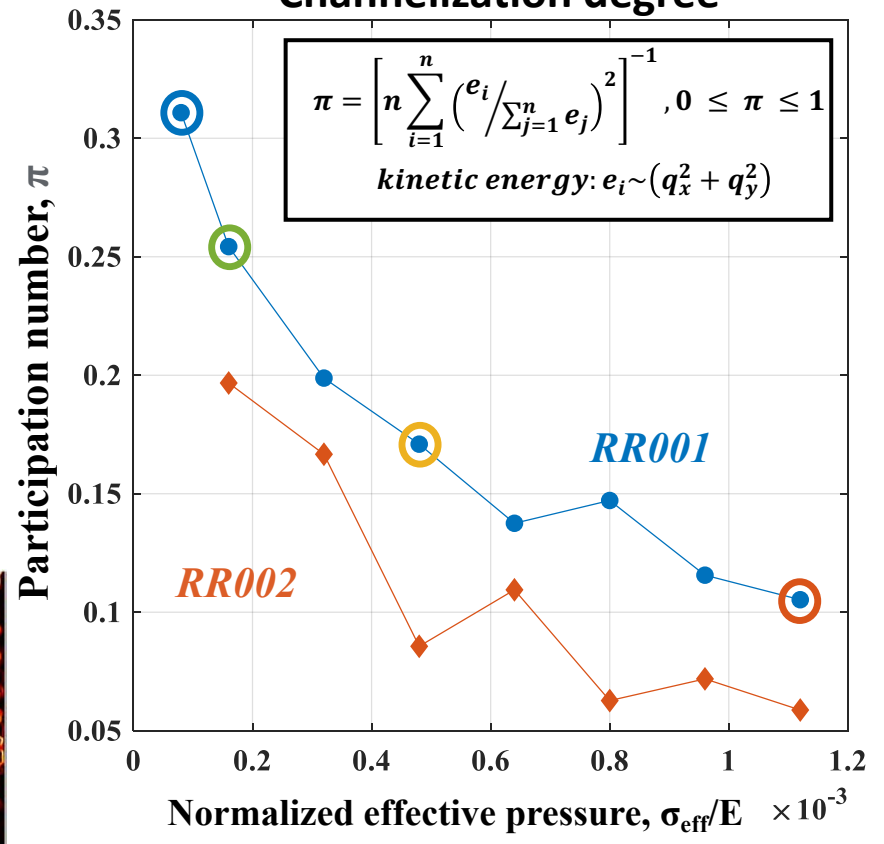
DETERMINATION OF THE FLOW FIELD: LOCAL CUBIC LAW



Increasing normal stress →

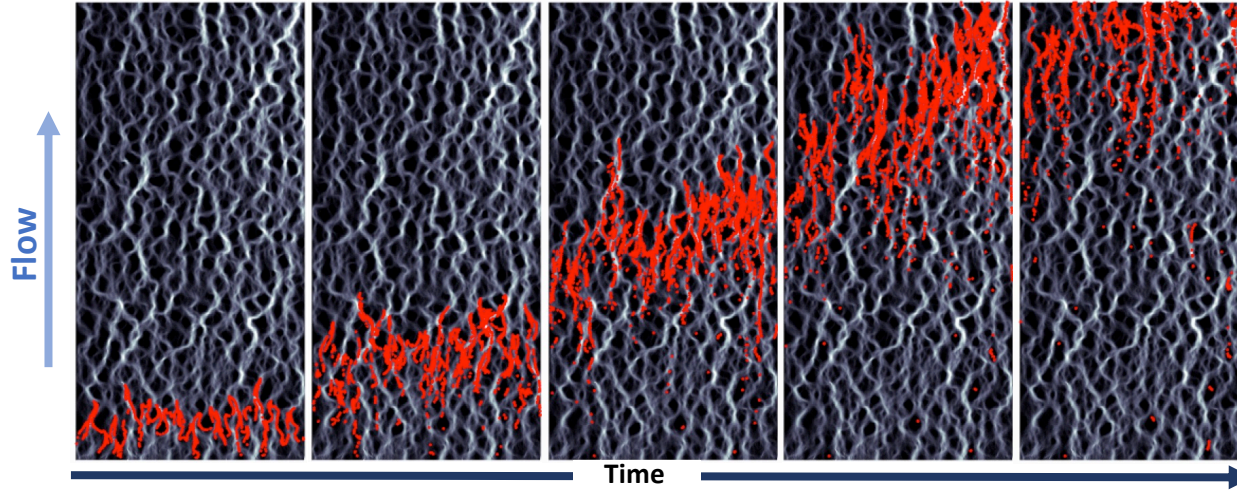
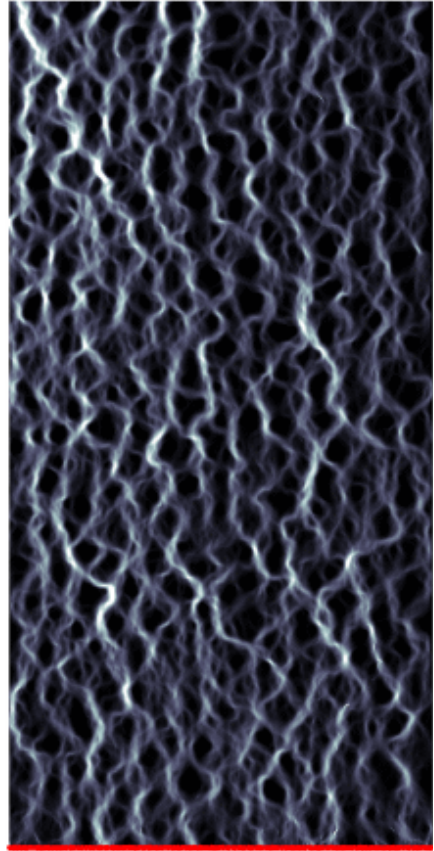


Channelization degree



Conservative Transport

PARTICLE TRACKING SIMULATIONS



Spatial Moments

$$M_1 = \langle x(t) \rangle = \frac{1}{N} \sum_{i=1}^N x_i(t) \longrightarrow \text{Center of mass}$$

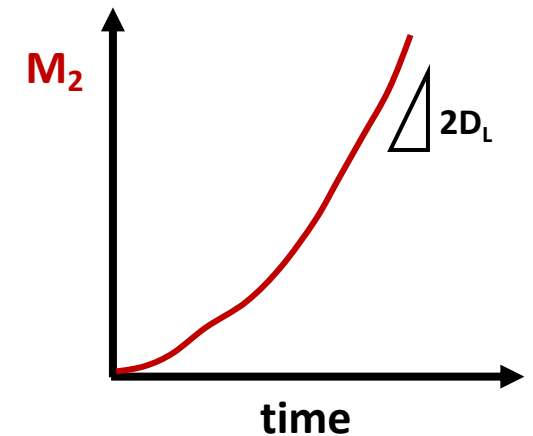
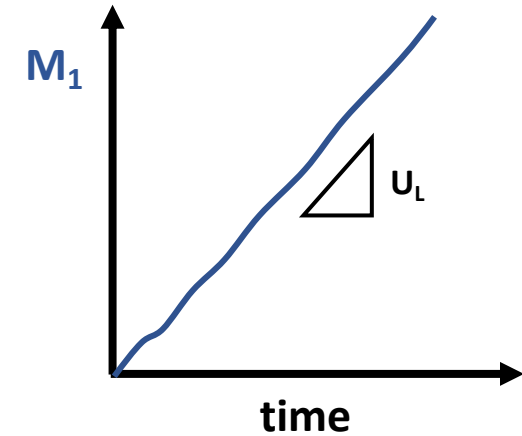
$$M_2 = \langle |x(t) - M_1|^2 \rangle = \frac{1}{N} \sum_{i=1}^N |x_i(t) - M_1|^2 \longrightarrow \text{Spread around the center of mass}$$

$x(t)$ Particle position

N Number of particles

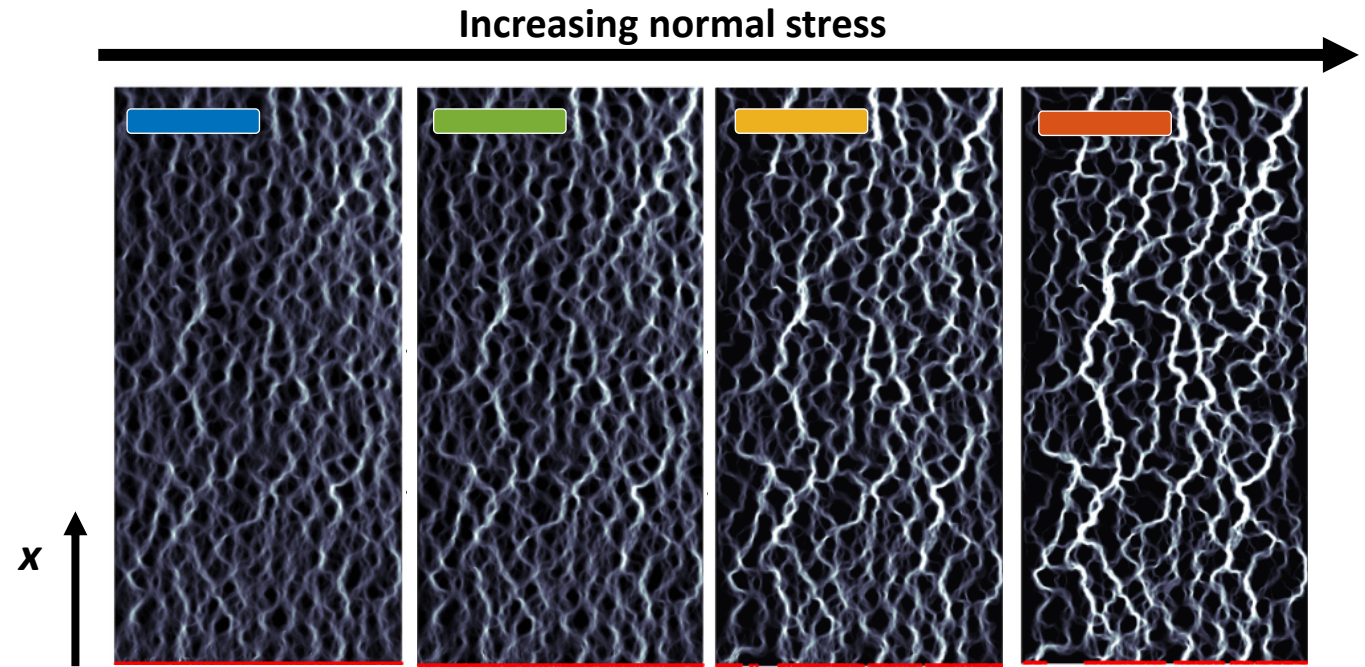
U_L Average velocity (longitudinal dir.)

D_L Dispersion coefficient (longitudinal dir.)



Conservative Transport

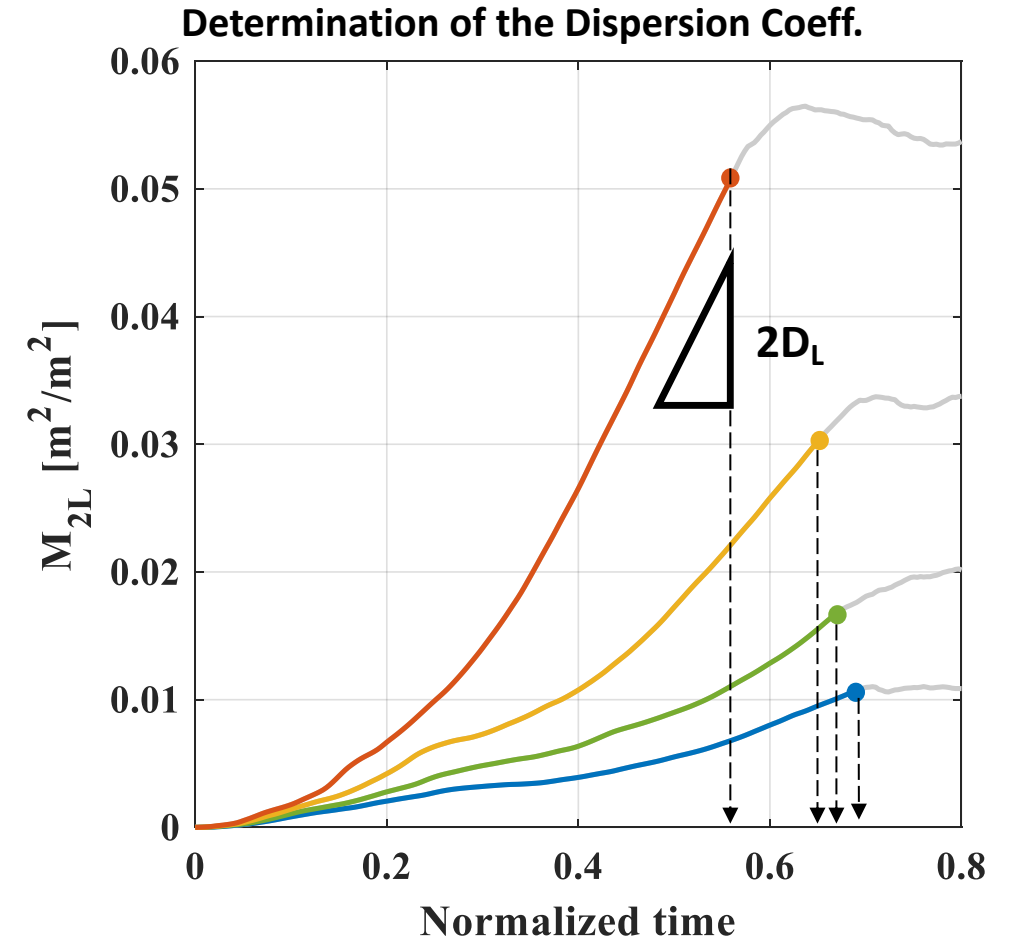
PARTICLE TRACKING SIMULATIONS



Spatial Moments

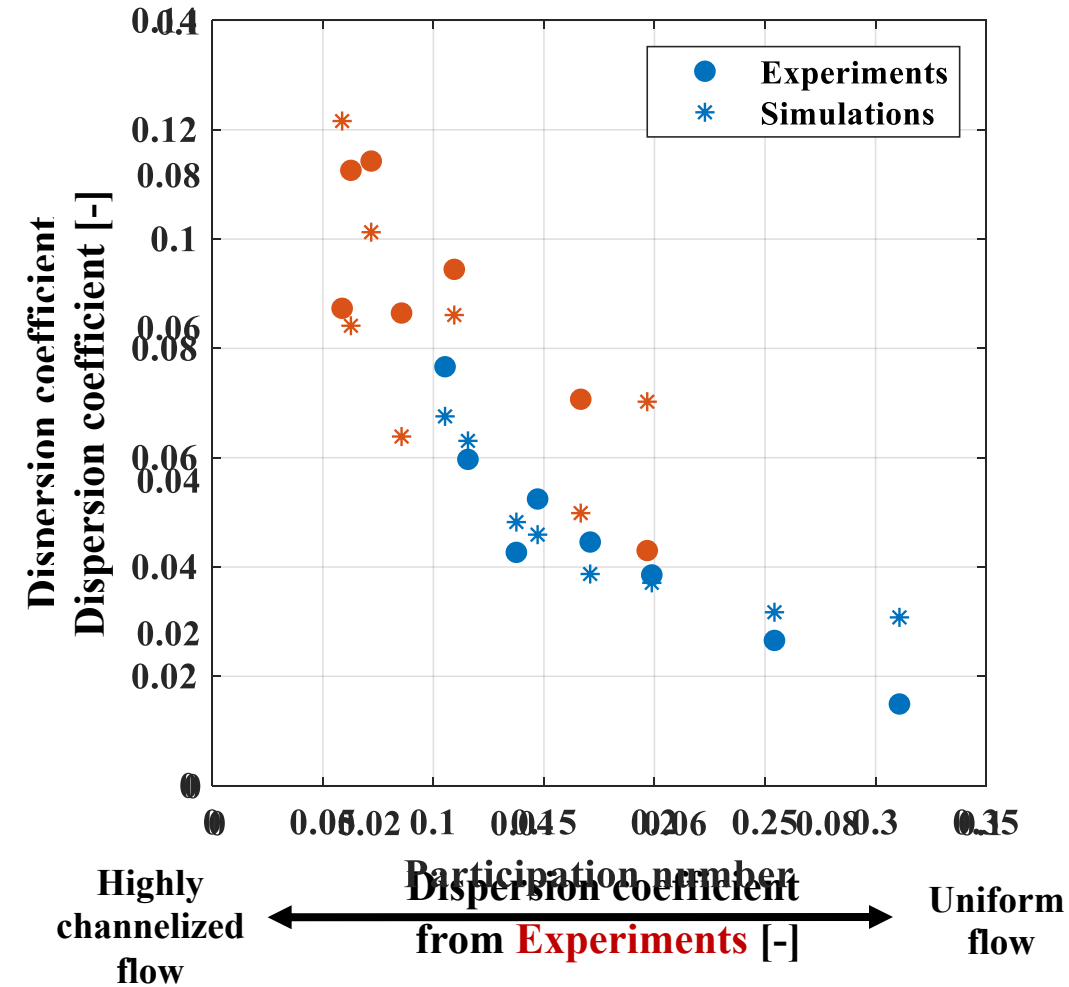
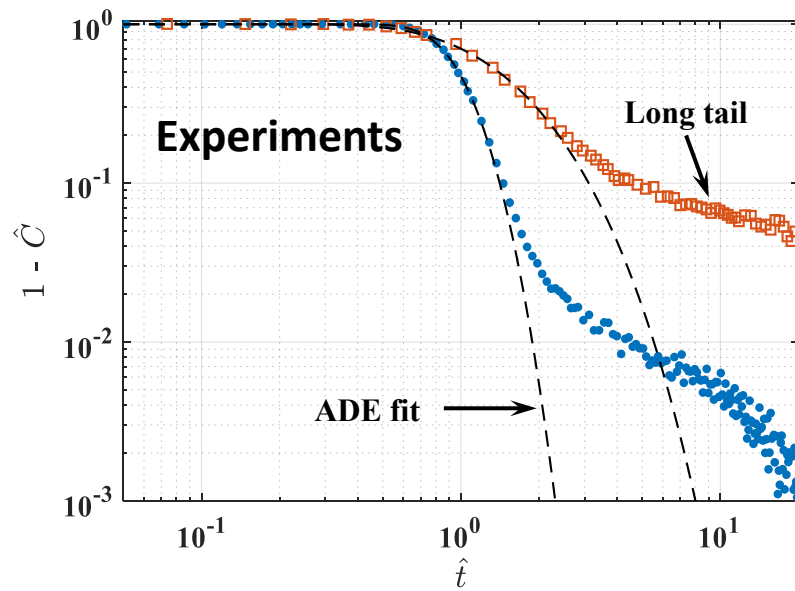
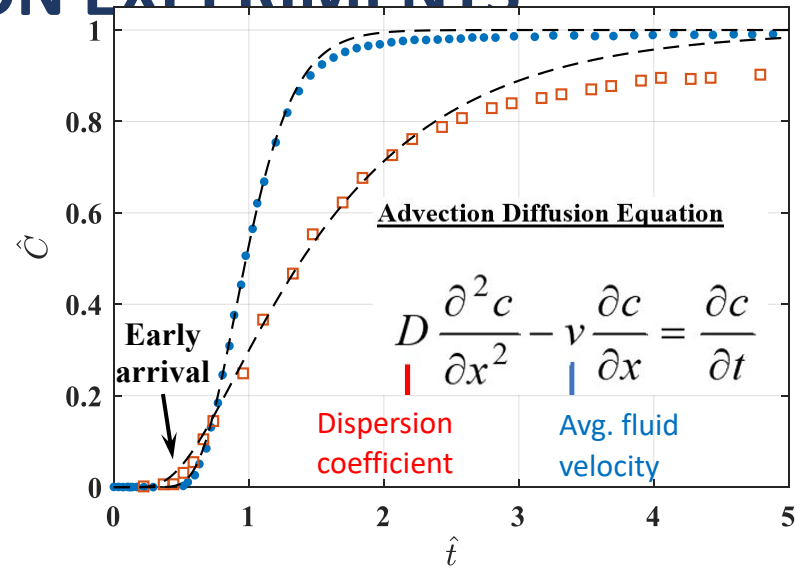
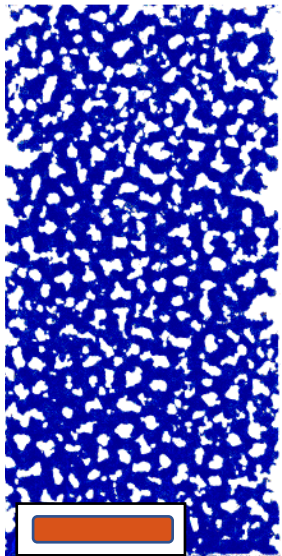
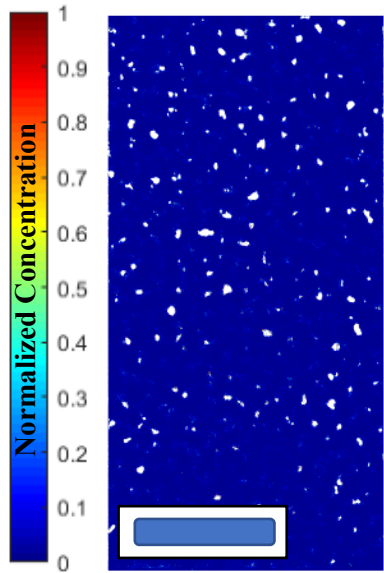
$$M_1 = \langle x(t) \rangle = \frac{1}{N} \sum_{i=1}^N x_i(t)$$

$$M_2 = \langle |x(t) - M_1|^2 \rangle = \frac{1}{N} \sum_{i=1}^N |x_i(t) - M_1|^2 \quad x(t) : \text{particle position}$$



Conservative Transport

TRACER INJECTION EXPERIMENTS



Conclusions

- Developed new experimental methodology combining digital fabrication of rock analogs and a novel pressure-controlled Hele-Shaw cell.
- In-situ measurement of aperture maps + geometric characteristics
- Stress-dependent permeability + flow field topology
- Evolution of mass transport dynamics

